On the Modelling of the Surface Meterological Variable Diurnal Cycles by Combined "Fuzzy Sets and Neural Networks"

Oleg M. Pokrovsky¹

Abstract

The joint statistical distribution of principal meteorological variables (temperature of air and soil, humidity of air and soil, atmospheric precipitation, pressure, shortwave radiation, cloudiness) are investigated. Ten years data sets of one hour temporal resolution for several meteorological sites of Russian North-West region are used. The data set of simultaneous observations (for all variables, seasons and sites) allows to reveal main features of joint diurnal distributions by means of the fuzzy set approach. Known and novel interrelationships between various meteorological and connected soil variables are reviewed. The revealed relationships between solar downward radiative fluxes and soil temperature diurnal patterns allow to simulate all principal elements of surface energy exchange :longwave outgoing radiative fluxes in the atmosphere, soil heat fluxes, sensible, turbulent and latent heat fluxes. It was found out that the most complicated links take place for fuzzy sets, corresponding to fractional cloudness diurnal patterns. There is an assymmetrical relationship between solar daily sums of radiance for half cloudy day and mean soil temperature values. That is a main cause for simulation of meteorological and heat balance component diurnal cycles in most ecological models. Introduced stationary and transition modes for main meteorological variable diurnal patterns represent the background for simulation of all known weather phenomena. This modes are used also as a neural network's nodes for hidden layers. Implementation of neural networks (back propagation algorithm) allows to perform several modelling experiments. Problem of optimum network configuration (number of nodes in hidden layers) is discussed. For example, it is possible to reconstruct the diurnal cycles of some meteorological variables with sufficient (at the observational error levels) precisions for each of them, by using 1, 2 or 3 instantaneous meteorological observations. Adapted nonlinear mapping of one group variables (and its diurnal distributions) on another one allow to investigate the possibility of application of this approach for diagnostical aims.

Potential applications of the developed approach are : downscaling in global models; spatial field reconstructions in case of missing observational data (for some variable(s));

¹ Main Geophysical Observatory, Karbyshev str.7, St.Petersburg, 194021, Russia e-mail: pokrov@main.mgo.rssi.ru

short-term forecasting; parametrization of energy exchange processes at the surface of the Earth.

1. Introduction

Various approaches and methods of simulation of meteorological processes at the surface of the Earth have been actively developed in recent years (e.g.Randall et al, 1991). The principal stimulus for these researches are linked with activation of regional and global climate change investigations, and also of complicated processes, occurring in ecosystems (Kondratyev et al, 1996, Pokrovsky, 1995, 1996).

The head stone for such researches is the study and simulation of diurnal cycle of basic near-surface meteorological parameters (air and soil temperature, humidity, pressure, precipitation, wind, cloud cover). In connection with necessity of description of energy exchange processes it is essential to consider also actinometrical parameters (downward and reflected SW radiation, outgoing LW radiation) (Cherveny et al, 1991, Kubota, 1991). During many years experts investigated specific features of a diurnal cycle of these parameters on the base of an empirical data (Cherveny/Belling, 1992; Thiao/Turpeinen 1992; Williams 1992). For cloud cover, examples of classification of diurnal or dayly distributions are represented in the literature (Berlyand, 1961; Zavjalov, 1990). The given problem for atmospheric temperature and humidity was traditionally considered at a qualitative level during many years. We mention some publications of last time (Klyuyeva 1990; Mass et al. 1991; Menzel 1992; Ruschy and Baker 1991). The examples of a classification of radiation characteristics at the surface of the Earth, mainly determined by distribution of a cloud cover, are presented in work (Flach, 1951; Flach, 1952). In last years activity in a ratio of study of a diurnal cycle of precipitation amount is exhibited (Haldar et al, 1991). It has allowed the authors to determine basic types of distributions and to make definite qualitative conclusions. Unfortunately, the majority of researches in this area is connected with study of a diurnal cycle of separate meteorological parameters. However, for simulation of complicated processes, taking place at the surface of the Earth, characterized by natural orography, it is necessary to investigate joint distribution of several parameters simultaneously.

On the other hand, there is the extensive literature (see, e.g. Cowan, 1968) on simulation of basic energy exchange processes at the surface of the Earth based on various forms of parametrization (radiative heating and cooling, sensible and latent heat transfer, turbulent heat exchange). These techniques are used not only in global climatic models, but have an independent value, as they can be applied in regional, as well as in ecological models. They are the most reliable tool for explanation of basic physical processes, occurring at the boundary layer :" atmosphere - surface of the Earth". However, the most of such models, as a rule, requires parameters which could be obtained from direct (contact) observations. Usually, optimal selection of

used parameters is a serious problem because of a lack of a full set of necessary observational data. Besides, for practical use of such models it is necessary to study temporal, for example, seasonal, intra-annual or interannual relationships of considered parameters. Dependencies on orography pecularities (vegetation cover, wood, presence of water reservoirs) is not less important. The last aspect explains the reason why, on the one hand, indicated methods of parametrization of processes at the surface of the Earth are used only beginning from intermediate term prognostic models, and, on the other hand, the short-term models, not using them, frequently don't satisfactorily reproduce diurnal cycles of such parameters as atmospheric temperature and relative humidity, which depend not only on an advection, but also on energy exchange processes in the "atmosphere - Earth surface" system. The presence of these problems, which are hard to overcome, is a reason for development of alternate methods of modeling of main meteorological processes at the surface of the Earth, based on use of all available ground-based network data archives (meteorological, hydrological, actinometrical, coastal marine and other).

In our opinion for solving this problems it is necessary to refuse from conventional methods of statistical analysis (calculations of moment, correlation functions, regression analysis and etc.), which ensure exposition only of linear relations. At the same time the most of meteorological processes and relationships should be referred (by their nature) to nonlinear. So our final goal is to describe this nonlinear processes by modern mathematical methods. The first step on a path should be the classification of basic meteorological parameter diurnal patterns by means of fuzzy logic (Jain/Dubes, 1988; Kohonen, 1989). Their diurnal cycles should be the object of the first phase of researches. Then it is necessary to proceed to classification of synoptic variability not only of single meteorological parameters, but also of their joint distribution to study their actual feedbacks.

In the first section of the paper the description of the used cluster analysis method is presented. The problem of classification of diurnal cycles of major meteorological parameters under condition of their statistical sample independence is further considered. In the third section the most actual problem - the study of joint probability distribution of several meteorological parameters for synchronized periods of observations and appropriate classification of linked diurnal cycles is considered. At the final section researches on classification of joint distribution of meteorological parameters on a time scale equal to two days are presented.

2. Fuzzy logic algorithm

In meteorology the large attention is given to the analysis of statistical relations between separate parameters. For study of their space and temporal distributions it is necessary to use methods of a multidimensional statistical analysis. One of the important direction is a combination of cluster and discrimination analysis. In the given research diurnal distributions of meteorological parameters will be considered. However, the offered approach can be applied to distributions of other temporal scales (monthly, seasonal, annual and etc.).

We shall assume that it is necessary to investigate a time scale, containing p - references (for example, instants of observations), and we arrange n - realizations of measurements in an indicated time interval. In this case measurement data can be presented as a matrix:

$$\mathbf{X} = \begin{bmatrix} X_{11} & X & \dots & X_{1n} \\ X_{21} & X_{22} & \dots & X_{2n} \\ \dots & \dots & \dots & \dots \\ X_{p1} & X_{p2} & \dots & X_{pn} \end{bmatrix} = (\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_n).$$
(1)

Each realization of the investigated process, represented by the vector - column X_{j} ,(j=1,..., n), can be interpreted as a point in Euclidean multidimensional space of size p. Using notation (1), it is possible to introduce several characteristics, describing scattering of data inside classes and a distance between classes. We define a matrix of size p * p

$$S_{x} = \sum_{i=1}^{n} (Xi - \overline{X}) (Xi - \overline{X})^{*}, \qquad (2)$$

(* - sign of a transposition)

It is named by a matrix of scattering of a observational set X, and $\overline{X} = \sum_{i=1}^{n} X_i / n$ is a vector of mean values. The trace of a matrix Sx, equal to a sum of diagonal elements, is named by statistical scattering of a set X.

The cluster analysis is based on partition of an initial set X on subsets, distance between which should be maximum. Now let us assume that there are two data sets X and Y. It is necessary to introduce a measure of a statistical distance between classes, formed by observational data matrixes X and Y:

$$\mathbf{D} = \boldsymbol{\alpha} \left(\overline{X} - \overline{Y} \right) * \left(\overline{X} - \overline{Y} \right), \tag{3}$$

where $\alpha = n1 n2 / (n1 + n2)$, n1, n2 - number of realizations in each class.

We shall enter into consideration a combined class Z=(X, Y). Relationship between scattering of observations inside class Z and corresponding values inside classes X and Y:

$$\mathbf{S}_{z} = \mathbf{S}_{x} + \mathbf{S}_{y} + \left(\left(\overline{X} - \overline{Y}\right) * \left(\overline{X} - \overline{Y}\right)\right),\tag{4}$$

is fundamental, as is used in any cluster analysis.

The equation (4) can be interpreted as follows: total scattering of two joint classes of realizations is equal to a sum of scattering inside classes and a distance between these classes(i.e. between its mean values). There are several fuzzy logic algorithms (Jain and Dubes, 1988). This algorithms are distinguished by that in one case the partition of a set of input object set into classes begins from one class, contained all objects, and in other, on the contrary, joining of separate objects into classes are performed by a selection of "nearest neighbors". We have used a method, concerning to the second group. The iterative algorithm implements under conditions of beforehand prescribed number of classes . Its essence is reduced to sequential search of objects from their initial distribution and to trial its transposition from one class to the other to acheive both a minimum of inside class scattering and a maximum of center to center class distance

3. Main meteorological parameter diurnal cycle modelling

A basis for our researches were archival hourly observational data for several sites of North-West region of Russia for 1984-93. The input data arrays, concerning to various meteorological parameters, were synchronized on time and presented separately for each of months. The calculations were carried out for several stations. The results of the classification have appeared similar. Therefore results for only one characteristic site Voejkovo (60 N, 30 E) are presented below.

Originally diurnal distributions, obtained by an independent way for atmospheric temperature and humidity, downward total (scattered plus direct) SW irradiance, atmospheric pressure, precipitation, direction and velocity of wind, were considered. Then rows of X-type matrix were performed. Each row contains diurnal distribution for a certain day. Thus for each parameter and each month a matrix was formed and the calculations on a partition of initial sample on a number of classes by means of cluster analysis, described above, were carried out. Calculations allowed to allocate each class as a set of distributions, minimum deviating in a Euclidean distance sense from average diurnal cycle (in a given class). As has been mentioned above the applied algorithm is aimed to maximize an Euclidean distance between mean value vectors, appropriate to diurnal pattern distributions of different classes. Despite a formal character of this algorithm, it has appeared, that the obtained outcomes have the reasonable physical interpretation.

We shall begin from reviewing diurnal cycle of total solar downward radiation. Its diurnal cycle in summer is the most significant due to amplitudes. Average (for 6 classes) distributions are shown at Fig.1. The obtained results suppose the simple interpretation. The upper curve corresponds to conditions of clear sky, and lower one to overcast cloud cover. Intermediate curves correspond to conditions of a fractional cloud cover, which can vary during a day (Table 1). For example, at forth class in the first half of a day the fractional cloud cover is of .3, and in the afternoon is of .7 and at fifth class the diurnal pattern has an opposite structure. It is necessary to note, that results of empirical classification of a day time cycle of cloud cover, presented in works (Flach, 1951; 1952), are closely interlaced with data from Table 1.

Cluster Number	Cloudness distribution
1	Clear sky - during a day
2	Clear sky -in the morning , fractional cloud cover of 0.3 - in the noon and the afternoon
3	Fractional cloud cover of 0.3 - in the morning and the noon, clear sky - in the afternon
4	Fractional cloud cover of 0.3 - in the morning , fractional cloud cover of 0.7 - in the noon and the afternoon
5	Fractional cloud cover of 0.7 - in the morning and the noon, fractional cloud cover of 0.3 - in the afternon
6	Overcasted cloudness - during a day

Table1 . Classification of cloudness and solar radiation diurnal patterns

To substantiate the interpretation of classification results presented in Table 1, parallel calculations of day time distribution of downward SW radiation for the latitude 60° and height of the Sun, adequate to appropriate month of the year, were performed. The calculations were carried out on the base of the Delta-Eddington approximation technique for homogeneous cloud model, with optical thickness equal to 30, the albedo of single scattering equal to 0.99 and asymmetry factor of the phase function g=0.85. The version of this technique for conditions of a fractional cloud cover, described in (Schmetz, 1984), was used. The values of fractional cloud cover given in Table 1 were selected by minimization of a divergence between calculated and empirical distributions of a day time cycle of radiation fluxes. It is interesting to note that cloud diurnal pattern classification results obtained in previous studies (see review at Berlyand, 1961) are closely linked to data given in Table 1. Fig.1b presents results of analogous classification for net radiation. The distributions show that net radiation diurnal pattern has the structure analogous to that obtained for surface solar irradiation (Fig.1a). This fact explains rather strong links between diurnal distributions of surface solar irradiation and near-surface temperature and other parameters, which will be discussed below.

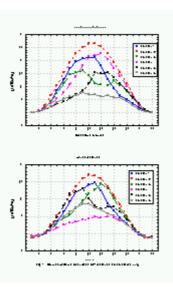


fig 1: diurnal cycle

Since a mathematical classification method is used, the question concerning the structure of each class can be arisen. Fig.2 shows the bands including the diurnal radiation distributions for two (from six) clusters (their "centers" are given at Fig.1a).

It is clear that classification can be considered a representative one not only if the class elements have minimal deviations from the center diurnal distribution (here it is mean values), but also if they have the same structure: coordinates of maximum and time gradient values. The given results demonstrate the fact that the proposed classification method guarantees precisely this similarity for most elements from the same class.

Let's consider a diurnal cycle of other meteorological parameters. For simplicity we will discuss the case of partition of initial sample onto 4 classes. Results of calculations (Fig.3) have shown, that in this case the obtained classes for temperature and humidity as well as for downwarn solar irradiance can be referred to two different groups. The first group includes distributions for which both parameters correspond to a stationary condition of atmosphere (i.e. during a day a considerable decrease or increase of parameter values deviations from multiannual average diurnal cycle is not observed).

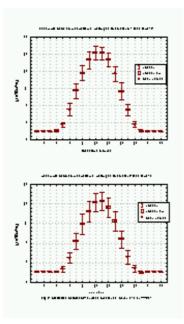


fig 2: bands

including the diurnal

Proceeding from these it is possible to name the appropriate average diurnal distributions as stationary modes. They are two and they correspond to keeping warm or cold weather pattern during the day. The second group includes classes, the average distribution of which, on the contrary, changes during the day compared to corresponding average diurnal cycles. Such distributions are possible to name as transient modes, as they follow the modifications of temperature and humidity in the course of the day. These modifications are connected with increasing or decreasing values of considered parameters. Curves, adequate to indicated types of modes, are showed on Fig.3. Four classes considered above allow to simulate closed loop variations of meteorological parameter during several sequential days, for example, synoptic variability. It is necessary to note that transient modes for solar radiation are mainly due to cloud cover varying in the course of the day.

radiation distributions

Typical diurnal patterns for other meteorological parameters shown on Fig.4 demonstrate the unlike characteristic type of relationships. So, for example, in case of low or high pressure(cluster 1 and 4) diurnal oscillations (Fig.4a) are more often observed. A study of precipitation has shown that rainfall before dawn, after midday and in the evening is the most probable. Moreover, the rain intensity increases in the indicated sequence and reaches a maximum at 19 o' clock of local sun time (Fig.4b).

Direction of wind is one of the most changeable and informative for the prognosis meteorological parameters. Fig.4ñ demonstrates its diurnal variability. From Fig.4c it follows, that the direction of wind is seldom saved during a day. The most probable modification time intervals are before dawn, in the morning, after midday and in the evening. In addition, the most intensive and quick are the changes from north-west wind to north-east, east and southern. Changes of southern wind to western are less intensive.

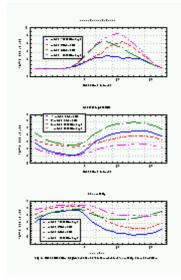


fig 3: bands including the diurnal radiation distributions

4. Diurnal cycle patterns of jointly distributed meteorological parameters

For a long time the problem of joint probability distribution of meteorological parameters attracts attention of meteorologists. However, till now in majority of studies authors limited themselves by only revealing of cross-correlations and constructing of regression models. Taking into account, that feedbacks in the atmosphere - Earth surface, atmosphere - cloud cover and other systems, determined by energy exchange processes have a nonlinear character, the above mentioned traditional statistical approaches, which involve only linear relations, give rather approximate conception on the essence of occurring processes.

The diurnal pattern of one or several meteorological parameters, corresponding to the given day can be represented as a point in a phase space of appropriate size. Our research has shown, that the points of such multidimensional phase space can be rather good classified, i.e. the input sample of points, adequate to empirical data, are splitted into an easily separated groups. It means that in the course of time a point, belonged to one cluster (adequate to one type of weather) is transferred to another cluster. For some time between these transpositions the point stays in the former cluster. It means that at this period the weather processes were stabilized. It is clear that the mentioned processes could not be accurately described by linear models.

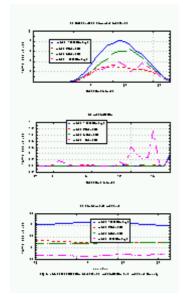


fig 4 : meteorological parameters

Let's consider outcomes of performed calculations. Results of joint diurnal patterns of three meteorological parameters: solar radiation, air surface temperature and humidity are similar to patterns, presented at fig.3. The chosen average distributions were divided rather conditionally into two groups of modes: stationary and transient ones. The sense of introduced terminology is obvious. Stationary modes correspond to the points in phase space, that are staying in the same cluster. Transient modes correspond to a transitional position of these points. The minimum number of clusters for this case is equal to 4. Stationary modes in a diurnal temperature and humidity cycles correspond to distribution of the clear sky radiation : maximum temperatures and minimum humidity and also maximum diurnal cycle amplitudes. Similarly other types of stationary modes of temperature and humidity correspond to radiation under conditions of continuous cloud cover. The difference is connected with minimum values of diurnal cycle amplitude. A varying fractional cloud cover corresponds to transient modes of temperature and humidity distribution. The indicated

transient modes describe passages from large to small values of meteorological parameters (temperature and humidity) and on the contrary.

The joint distribution of total solar radiation, precipitation and atmospheric pressure (Fig.5) demonstrates their coherence. At the clear sky conditions (Fig.5a) high pressure (Fig.5c) and absence of precipitation (Fig.5b) are observed.

In this case one finds two distributions corresponding to conditions of overcasted cloud cover (Fig.5a, curves 2 and 4). Thus, curve 2 corresponds to distribution, associated with decrease of pressure (Fig.5c). On the contrary, continuous cloud cover (Fig.5a, the curve 4) at low pressure corresponds to the curve 4 on Fig.5b, revealing the presence of precipitation. Pattern, describing increase of pressure and absence of precipitation corresponds to distribution of radiation at a fractional cloud cover. Practically it is possible to speak about two classes of distributions for precipitation: days with rainfall and without rainfall.

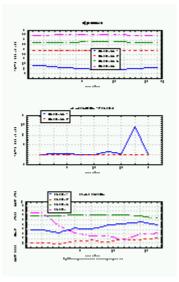


fig 5: joint distribution of total solar radiation, precipitation and atmospheric pressure

The clusterization of joint distribution of main meteorological parameters - pressure, precipitation and wind direction also gives characteristic correlations of a diurnal cycle. High pressure is accompanied by the lack of precipitation and western direction of a wind with passage to southern and south-eastern direction. At lower pressure (curve 3 at fig.4à) the precipitation is also absent, and the wind has mainly western direction. At a further drop of pressure (the curve 2 at fig.4a) wind has

mainly south-eastern direction. At low pressure (the curve 1 at fig.4a and fig.4c) precipitation is observed, and wind changes from southern to western direction. In July the increasing pressure curve corresponds to "no" precipitation and to probable change of wind from west to south and southwest direction. Providing lower pressure, precipitation is absent too, but wind has prevalent southeast or northeast direction. The decreasing pressure curve corresponds to higher probability of precipitation and wind changes from south to west direction

Mentioned results allow to make some conclusions. The typical diurnal cycle of basic meteorological parameters is characterized by consistent distribution of either stationary or transient modes. Fundamental influence of solar radiation on atmospheric temperature and humidity becomes more clear. Characteristic pressure distributions and appropriate distributions of precipitation and wind directions specify certain weather conditions and their modifications. Analogue conclusions are obtained for relations between cloud cover and precipitation. The number of clusters could be enlarged for more detail description of other weather conditions. The obtained classification could form a basis for a solution of both fundamental and applied problems. To the first group it is possible to refer the problem of modeling of a diurnal cycle of meteorological parameters, and the problem of the short-term weather forecasting or automatic monitoring of observational data could be referred to the second group.

5. Modelling of the multidiurnal variability of jointly distributed meteorological parameters

Modifications of weather conditions occur not only during day period, but also consecutive days on a synoptic temporal scale. Therefore the problem of clusterization of two and three-diurnal joint distributions of basic meteorological parameters was considered. Here as well as above we are interested to study the stationary and transient modes . Therefore only 4 classes for joint distribution of solar radiation, temperature, humidity and precipitation were selected for a minimum model. The major interest represents a role of joint distribution of parameters. Fig.6 demonstrates the clusterization results of two-diurnal patterns of joint radiation, temperature and humidity distributions. As it was mentioned above the stationary modes illustrate preservation of two types of distributions at passage from the first day to the second. There are two modes of such kind: keeping cold or warm weather types(curve 1 and 3). On the contrary, the transient modes describe modifications of weather conditions. Passage from the clear sky conditions (the curve 2, Fig.6à) to the overcast cloud cover results in the decreasing of temperature (curve 2, Fig.6b) and increasing of relative humidity (curve 2, Fig.6c). Passage (the curve 4, Fig.6à) from the continuous cloud cover to the clear sky leads to the inverse variations of the rest parameters, i.e. raise of temperature and drop of humidity. Once again it proves the determining role of radiation processes, controlled by a cloud cover.

Independent distribution of basic meteorological parameters on an interval equal to two days looks similar to considered above case of joint distribution of parameters. However, obtained modes are not completely logically matched. It means, for example, that transient modes of one parameter can fit similar modes of another parameter, more appropriate by physical reasons to other modes.

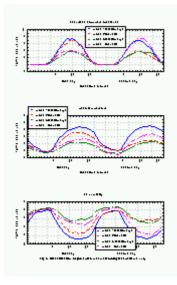


fig 6: describe modifications of weather conditions

6. Conclusion

The obtained results principally differ from conventional studies on statistical features of meteorological parameters widely represented in scientific literature. The conventional approaches are usually based on application of correlation or regression analysis techniques, which are linear by their nature. These methods usually deal with norms of meteorological parameters and statistical estimates of deviations from these norms. In this case it is possible to get estimates of deviations of some parameters as a linear function of the other. It concerns both diagnostic, and prognostic problems. However, determination of an area of applicability of linear methods and emerging of new techniques of nonlinear process modeling, developing in parallel to significant progress of computer facilities, give stimulus for application of nonlinear methods for statistical description of meteorological values and fields. Here first of all we mean the " neural network" techniques, which originally emerged from the problems of an artificial intelligence and obtained broad spreading at a solution of many applied problems in various branches of science and engineering. Applying "neural network" methods (Allen and Le Marshall,1994; Bankert and Aha, 1996) it is necessary first of all to define cells or nodes of such network. The purpose of the given work consists not only in study of non-stationary diurnal and multidiurnal oscillations (modes), but also in the definition of elementary neural network for modelling diurnal cycles and multidiurn alatterns of main meteorological parameters. Thus, it is possible to consider the present research as the introduction to the application of new computing techniques for simulation of nonlinear meteorological processes observable at the surface of the Earth.

Bibliography

- Allen, G., Le Marshall, J. F. (1994): An evaluation of neural networks and discriminant analysis methods for application in operational rain forecasting. -Australian Meteorological Magazine, v. 43,1, p. 17-28.
- Bankert, R. L. and Aha, D. W. (1996): Improvement to a neural network cloud classifier. -Journal of Applied Meteorology, v. 35, p. 2036-2039.
- Belling R.C. and Idso S.B. (1991): Decreasing diurnal temperature range : CO₂ greenhouse or SO₂ energy balance effect ? - Atm.Research, v.26, 5, p.455-459.
- Berlyand M.E. (1956): Forecasting and Regulation of Heat Regime of Atmospheric Boundary Layer, Leningrad., Hydrometeoizdat., 435 p(in Russian).
- Berlyand T.G.(1961): Sun Radiance Distribution at Continents. ., Leningrad., Hydrometeoizdat. , 227 p.(in Russian).
- Cherveny R.S., Belling R.C. (1992): The impact of snow cover on diurnal temperature range.-Geoph.Res.Let., v.19, 8, p.797-800.
- Cherveny R.S.(et al) (1991): Outgoing longwave radiation and its diurnal variation from combined ERBE and Meteosat observations 2 : Using Meteosat data to determine the longwave diurnal cycle.- J.Geoph.Res., v. 96, D.12, p.22623-22630.
- Cowan I.R. (1968): Mass, heat and momentum exchange between stands of plant and their atmospheric environment.-Quart.J.Roy.Met.Soc.,v.94, p.523-544.
- Flach E. (1951): Zum Taglichen und Jahrlichen Gang der Bewolkung. Zeitschr. fur Meteorologie, H. 7-8, p.645-656.
- Flach E. (1952): Tages und Jahreszeitliche Besonderheiten in Verhalten der Bewolkung. Zeitschr. fur Meteorologie, H. 1-2, p.21-32.
- Haldar G.C.(et al) (1991): Diurnal variation of monsoon rainfall.- Mausam(New Dehly), v.42,1 , p.37-40.
- Jain A.K., Dubes R.C. (1988): Algorithms for clustering data., Prentice Hall, 234 p.

- Joseph J.H.(et al) (1976): The Delta-Eddington approximation for radiative flux transfer, J.Atmos. Sci., v. 33, p. 2452-2459
- Klyuyeva Ì.V. (1990): Calculated maximum of air temperature.- Trudy GGÎ, issue 532, pp.91-96.(in Russian).
- Kohonen T. (1989): Self Organization and Associative Memory.Springer Verlag, 342 p.
- Kondratyev K.Ya.(et al) (1996): Global Change:Remote Sensing. Chichester,J.Wiley and Sons,Praxis Publ.,370 p.
- Kubota I. (1991): Diurnal variation of radiation, measured by GMS J. of Meteorol.Res.(Tokyo), v.43, 3, p.71-97.
- Kukla G., Karl T.R. (1992): Recent rise of the nighttime temperature in the Northern Hemisphere.-Oak Ridge, TN, CDIAC, ECD, Oak Ridge National Lab., p.4.
- Mass C.F.(et al) (1991): Diurnal surface-pressure variations over continental United States and influence of sea level reduction. Monthly Weather Rev., v.119, 12, p.2814-2830.
- Menzel W.P.(1992): Seasonal and diurnal changes in cirrus clouds as seen in four years of observations with VAS. J. Apl.Meteorology, v.31,4 , p.370-385.
- Pokrovsky O.M. (1995): The Modelling of Ecodynamic and the Optimal Design of Measurement System.- Earth Research from Space, N 4, ñ.35-44 .(in Russian, translated into English).
- Pokrovsky O.M. (1996): Ecological Resistance Model and Environmental Monitoring Reports of Russian Acad of Sci.,v.346, N 6, ñ.819-821.(in Russian, translated into English).
- Randall, D. A.(et al) (1991): Diurnal variability of the hydrological cycle in a general circulation model. - J. Atmos. Sci., v.48, 1, p. 40-62.
- Ruschy D.L., Baker D.G. (1991): Seasonal variations in dayly temperature ranges.-J. of Climate, v.4,12, p.1211-1216.
- Schmetz J. (1984): On the Parametrization of the Radiative Properties of Broken Clouds.-Tellus, v.36a, p. 417-432.
- Thiao W., Turpeinen O.M. (1992): Large-scale diurnal variations of tropical cold cloudiness based on a simple cloud indexing method. J. of Climate , v.5, 2, p.173-180.
- Williams C.R. (1992): Comparison of observed diurnal and semidiurnal tropospheric winds at Christmas Island with tidal theory. -Geophys.Research.Let., v.19, 14, p.1471-1474.
- Zavyalov P.Î. (1992): Cloudness impact on diurnal surface ocean temperature variations.-Meteorology and Hydrology, 4, p. 61-67.(in Russian, translated into English).